



$A \rightarrow \text{Yes Sir}$
 $B \rightarrow \text{No Sir}$

$A \rightarrow \text{Yes}$
 $B \rightarrow \text{No}$

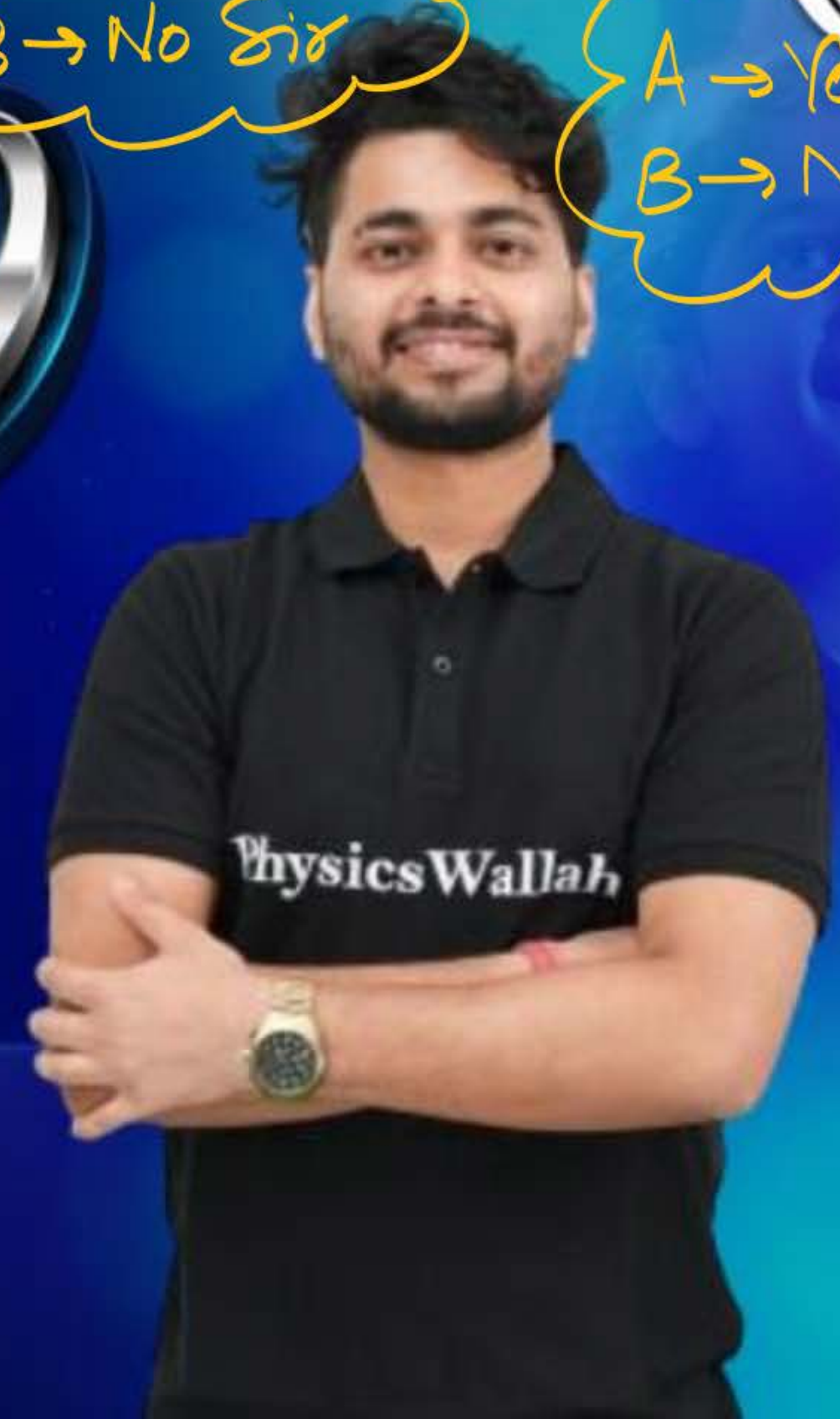


Class 10th Basics (Part - 03)

Maths

Lecture - 03

By – Prince Sensei Sir



Topics

to be covered

1 Game of signs (continued)

2 Formula Magic

3 Graphs

$$(-) + (-) = (-)$$

$$(-2) + (-5)$$

$$= -2 - 5 = (-7)$$



Recap

of previous lecture

1 Prime Factors & its usefulness

2 Game of signs

$A \rightarrow \text{Lec-I}$

$B \rightarrow \text{Lec-II}$

$C \rightarrow \text{Lec I \& II}$

$D \rightarrow \text{None}$





Game of sign



$$2 \times 6 = 12$$

* Analysing $(\alpha \cdot \beta)$

i) Case I

$$\alpha \rightarrow (+)$$

$$\beta \rightarrow (+)$$

Solⁿ

a) (+)

b) (-)

c) can be (+) or (-)

d) none

$$\Rightarrow \boxed{\alpha \cdot \beta} \rightarrow (+) \times (+) = (+)$$

α, β

$$\alpha + \beta$$

$$\alpha \otimes \beta$$

$$\alpha \odot \beta$$



Game of sign



Sign

Tutsu

Example

* Analysing $(\alpha \cdot \beta)$

22) Case II

$\alpha \rightarrow (-)$

$\beta \rightarrow (-)$

$$(-3) \times (-7) = +21$$

Solⁿ

a) (+)

b) (-)

c) can be (+) or (-)

d) none

Solⁿ

$$\Rightarrow \begin{array}{c} \alpha \cdot \beta \\ \downarrow \quad \downarrow \\ (-) \times (-) = (+) \end{array}$$

*

$$\boxed{\begin{array}{ccc} \square & \times & \square \\ \text{Same sign} & & \end{array}} = (+)$$

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Game of sign



* Analysing $(\alpha \cdot \beta)$



$$5 \times (-3) = -15$$
$$3 \times (-5) = -15$$

Solⁿ

a) (+)

☒ b) (-)

c) can be (+) or (-)

d) none

$$\begin{array}{cc} \alpha & \cdot & \beta \\ \downarrow & & \downarrow \\ (+) & \times & (-) = (-) \\ (-) & \times & (+) \end{array}$$



Game of sign



* Analysing $(\alpha \cdot \beta)$



Solⁿ

a) (+)

☒ b) (-)

c) can be (+) or (-)

d) none

$$(-2) \times 8 = -16$$

$$\alpha \cdot \beta$$
$$(-) \times (+) = (-)$$

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$$\square \times \square \rightarrow (-)$$

Opp sign

Wants

QUESTION

$$2+4=6$$

$$-2+(-4)$$

$$=-6$$

same sign

$$\square + \square \rightarrow +, -$$

$$\square \times \square \rightarrow (+)$$

* If γ, δ are of the same sign, then $\left(\frac{\gamma+\delta}{\gamma \cdot \delta}\right)$ is ?

A (+)

B (-)

C ☒ may be (+) or (-)

D none

Soln

$$\frac{(\gamma+\delta)}{(\gamma \cdot \delta)} \rightarrow \frac{(+)/(-)}{(+)}$$

$$\Rightarrow \frac{(+)}{(+)} \quad \bigg| \quad \frac{(-)}{(+)}$$

$$\Rightarrow (+) \quad \bigg| \quad (-)$$



QUESTION



Q. If a & b are of opposite signs, then what can be said about the product of a & b ?

A (+)

B (-)

C may be (+) or (-)

D none

Sol: $\boxed{a \cdot b} \xrightarrow{\text{opp signs}} (-)$



Formula Magic



i) $(a+b)^2 = a^2 + b^2 + 2ab$

$(a+b) \cdot (a+b)$

$a^2 + \underbrace{ab + ab}_{2ab} + b^2$

Twist //

$(a+b)^2 = \underbrace{a^2 + b^2} + 2ab$

$(a+b)^2 - 2ab = a^2 + b^2$

* $\boxed{a^2 + b^2 = (a+b)^2 - 2ab}$

$\boxed{(\text{साधा})^2 + (\text{घोडा})^2}$

$\rightarrow (\text{साधा} + \text{घोडा})^2 - 2 \times \text{साधा} \times \text{घोडा}$

QUESTION



*

* Q If $(a+b)=6$ & $ab=3$, find (a^2+b^2)

- A 36
- B 6
- C 30
- D none

Sol: $a^2+b^2 = (a+b)^2 - 2ab$
 $= (6)^2 - 2 \times 3$
 $= 36 - 6$
 $= 30$



Formula Magic



1) $(a-b)^2 = a^2 + b^2 - 2ab$

$$= (a-b) \times (a-b)$$

$$= a^2 - \underbrace{ab - ab}_{-2ab} + b^2$$

$$\left. \begin{array}{l} a+b \\ a \cdot b \end{array} \right\} \begin{array}{l} a-b=3 \\ a \cdot b=5 \end{array}$$

$$\rightarrow a^2 + b^2 + 2ab + (a^2 + b^2 - 2ab)$$

$$\rightarrow \underline{a^2} + \underline{b^2} + \cancel{2ab} + \underline{a^2} + \underline{b^2} - \cancel{2ab}$$

$$\rightarrow 2a^2 + 2b^2$$

$$\rightarrow 2(a^2 + b^2)$$

Way I

Way II

$$\begin{aligned} (a^2 + b^2 + 2ab) - (a^2 + b^2 - 2ab) \\ \cancel{a^2} + \cancel{b^2} + 2ab - \cancel{a^2} - \cancel{b^2} + 2ab \\ = \underline{4ab} \end{aligned}$$

$$(a-b)^2 = \underline{a^2 + b^2} - 2ab$$

$$\Rightarrow (a-b)^2 + 2ab = a^2 + b^2$$

$$\Rightarrow \underline{a^2 + b^2} = (a-b)^2 + 2ab$$

$$\rightarrow (a+b)^2 + (a-b)^2 = 2(a^2 + b^2)$$

$$* (a+b)^2 - (a-b)^2 = 4ab$$

* New

New ✓



Formula Magic



$\circledast$

$$\begin{aligned} \text{ii)} \quad (a+b)^3 &= a^3 + b^3 + \boxed{3a^2b + 3ab^2} \\ &= a^3 + b^3 + \boxed{3ab(a+b)} \end{aligned}$$

$\rightarrow 3ab(a+b)$

$$(a+b)^3 = \boxed{a^3 + b^3} + \boxed{3ab(a+b)}$$

$$(a+b)^3 - 3ab(a+b) = a^3 + b^3$$

$$\ast \quad \boxed{a^3 + b^3 = (a+b)^3 - 3ab(a+b)} \quad \ast$$

$$\Rightarrow \boxed{a^3 + b^3 = (a+b)(a^2 + b^2 - ab)}$$

$$\Rightarrow \boxed{(4161)^3 + (6151)^3}$$

QUESTION



*

* Q If $a+b=1$ & $ab=2$, find $(\underline{a}^3 + \underline{b}^3)$

*

A

1 ☐

B

2 ☐

C

3 ☐

D

none / none of these
none of above

Solⁿ:

$$a^3 + b^3 = (\underline{a+b})^3 - 3\underline{ab}(\underline{a+b})$$

$$= (1)^3 - 3 \times 2 \times 1$$

$$= 1 - 6$$

$$= \boxed{-5}$$



Formula Magic



$$\text{iv) } \underline{(a-b)^3} = a^3 - b^3 - 3a^2b + 3ab^2 \\ = a^3 - b^3 - 3ab(a-b)$$

$$\begin{aligned} & -3a^2b + 3ab^2 \rightarrow (-) \times (-) \\ & -3ab(a-b) \end{aligned}$$

$$(a-b)^3 = \underbrace{a^3 - b^3}_{\text{}} - \underbrace{3ab(a-b)}_{\text{}}$$

$$(a-b)^3 + 3ab(a-b) = a^3 - b^3$$

Less

$$\boxed{a^3 - b^3 = (a-b)^3 + 3ab(a-b)} \\ = (a-b)(a^2 + ab + b^2)$$

$$(1111)^3 - (1111)^3$$



Formula Magic

$(a, b), c$ $\times$ 98%



* $a^3 + b^3 + c^3 - 3abc = (a+b+c)(a^2 + b^2 + c^2 - ab - bc - ac)$

0

* $a^3 + b^3 + c^3 - 3abc = 0$

* $a^3 + b^3 + c^3 = 3abc$

a^3, b^3, c^3

QUESTION



*Q If $a+b+c=0$, then, $(\overset{3}{a} + \overset{3}{b} + \overset{3}{c}) = ?$

- A abc
- B $2abc$
- C $3abc$
- D Don't know

L-1
L-2
L-3

*

